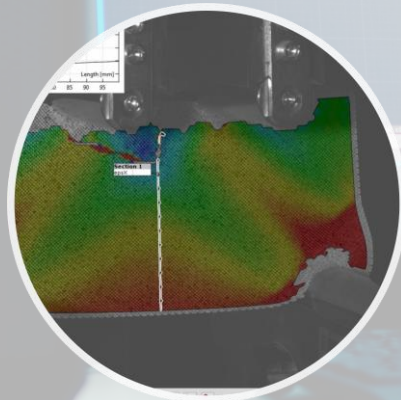
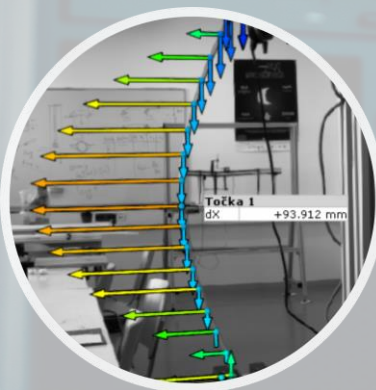
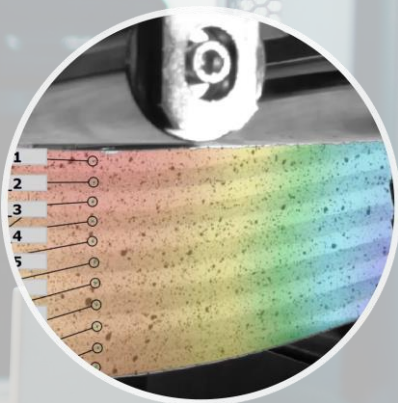


PROGRAM MIKROKVALIFIKACIJE:

# PRIMIJENJENA MEHANIKA U SUVREMENOJ INŽENJERSKOJ PRAKSI



G

F

Sveučilište  
u Rijeci  
Građevinski  
fakultet

PROGRAM MIKROKVALIFIKACIJE:

# PRIMIJENJENA MEHANIKA U SUVREMENOJ INŽENJERSKOJ PRAKSI



diplomski studij  
**Građevinarstvo**  
smjer **Konstrukcije**

**4 izborna predmeta**  
u 2. semestru

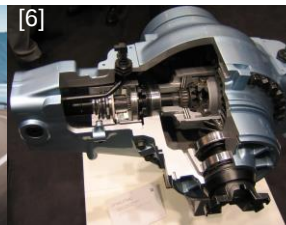
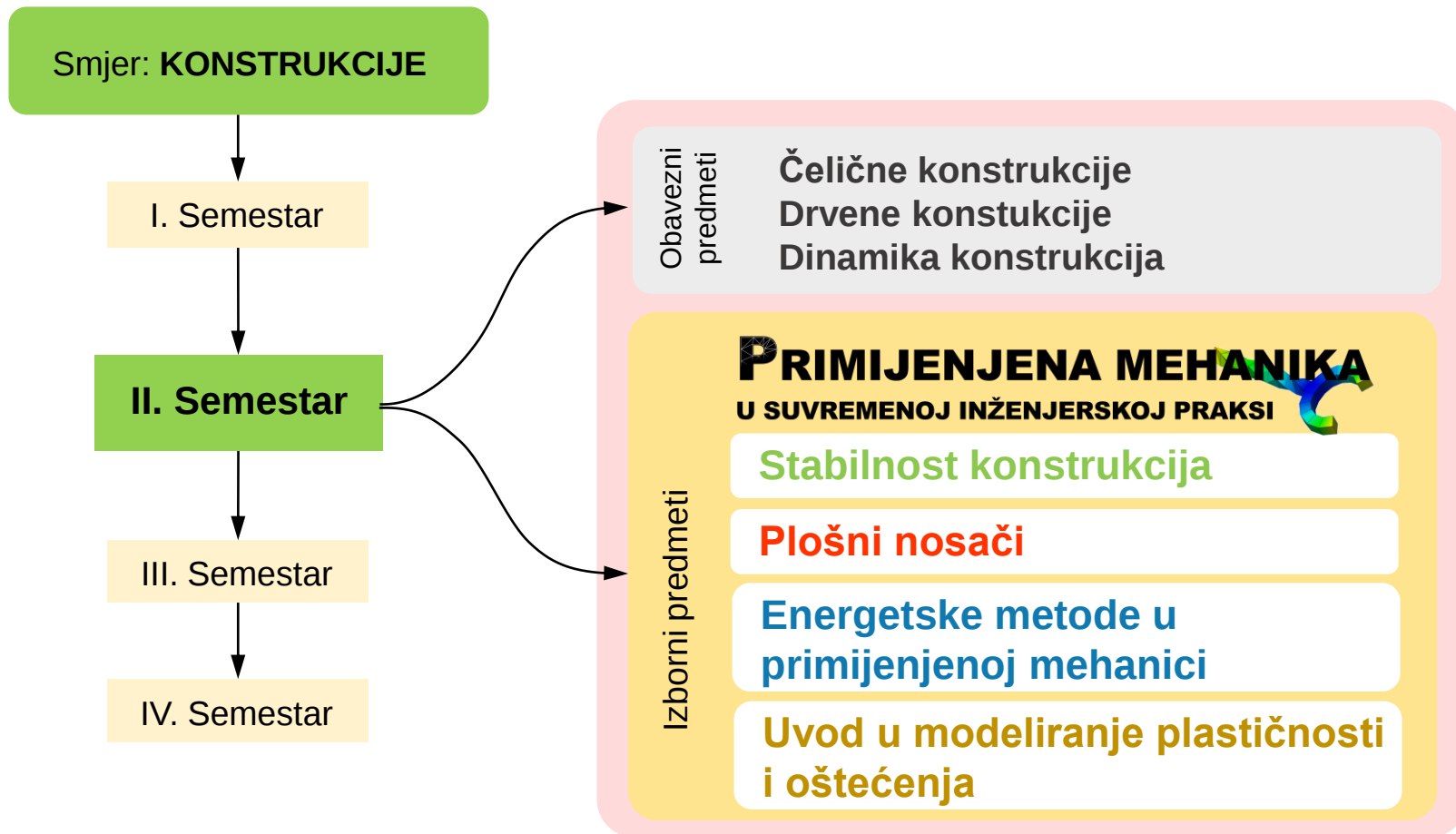
može se  
upisati kao  
**program**  
**cjeloživotnog**  
**učenja**  
(dostupan onima koji  
nisu studenti)

može se slušati na  
**engleskom**  
**jeziku**  
(preporučljivo)

stjecanje  
**znanja, vještina**  
**i kompetencija**  
+  
**nove mogućnosti**  
**zapošljavanja**

izdavanje  
**potvrde o**  
**završenom**  
**programu**

# Diplomski sveučilišni studij GRAĐEVINARSTVO



## ECTS bodovi

Stabilnost konstrukcija

4

Plošni nosači

3

Energetske metode u  
primijenjenoj mehanici

3

Uvod u modeliranje plastičnosti  
i oštećenja

4

**PRIMIENJENA MEHANIKA**  
U SUVREMENOJ INŽENJERSKOJ PRAKSI

14

+

Obavezni predmeti

16

II. Semestar ukupno:

30



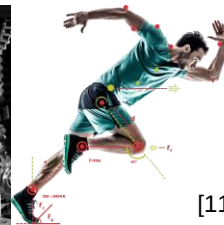
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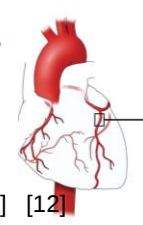
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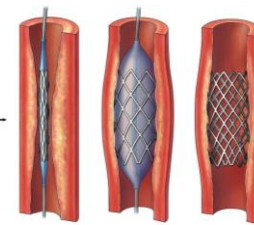
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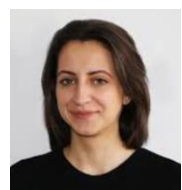
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[12]

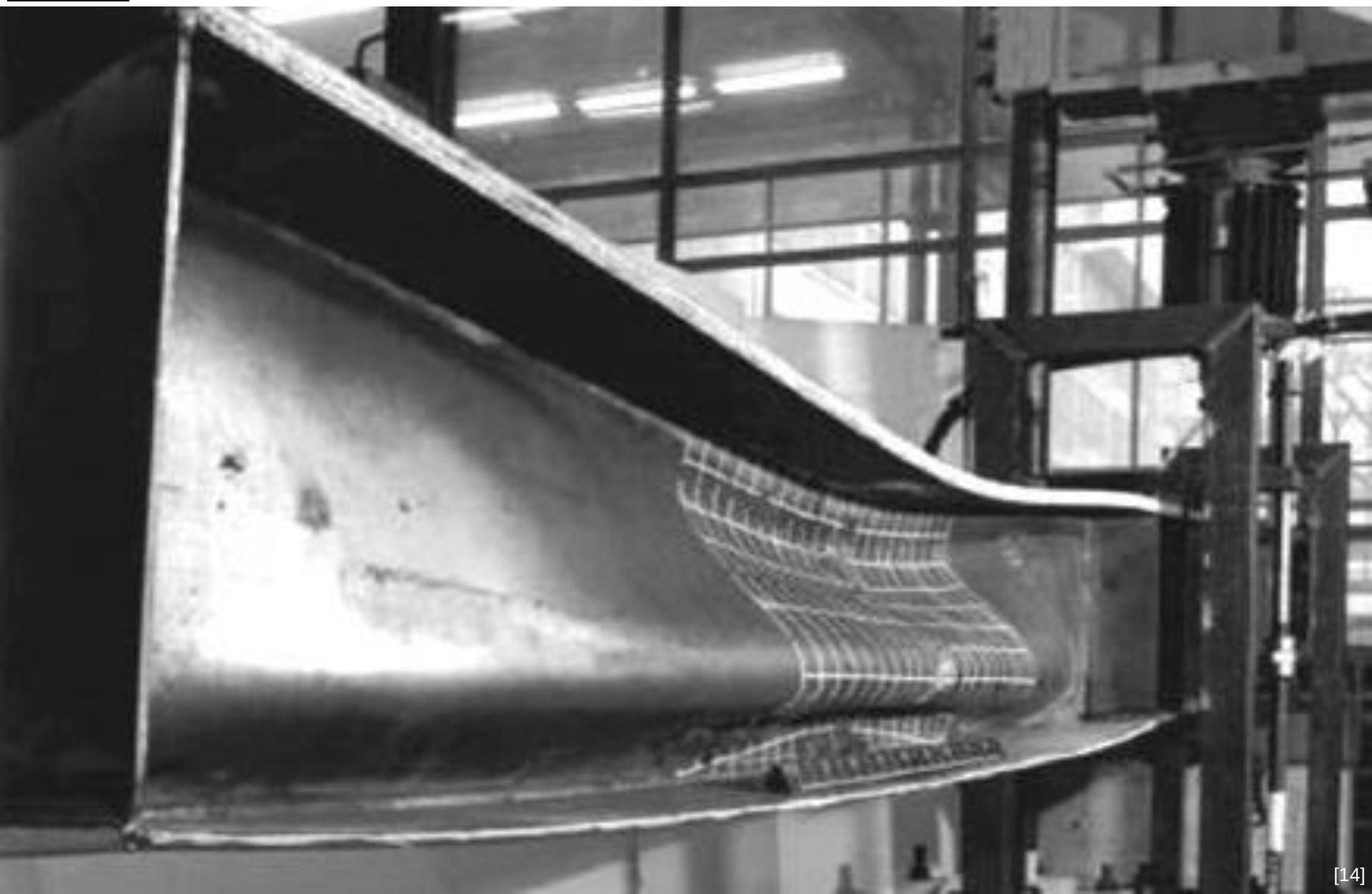


[13]



izv. prof. **Emina Hadžalić**  
[emina.hadzalic@uniri.hr](mailto:emina.hadzalic@uniri.hr)  
G-328

# Stabilnost konstrukcija



# Stabilnost konstrukcija



[15]



[16]

[17]

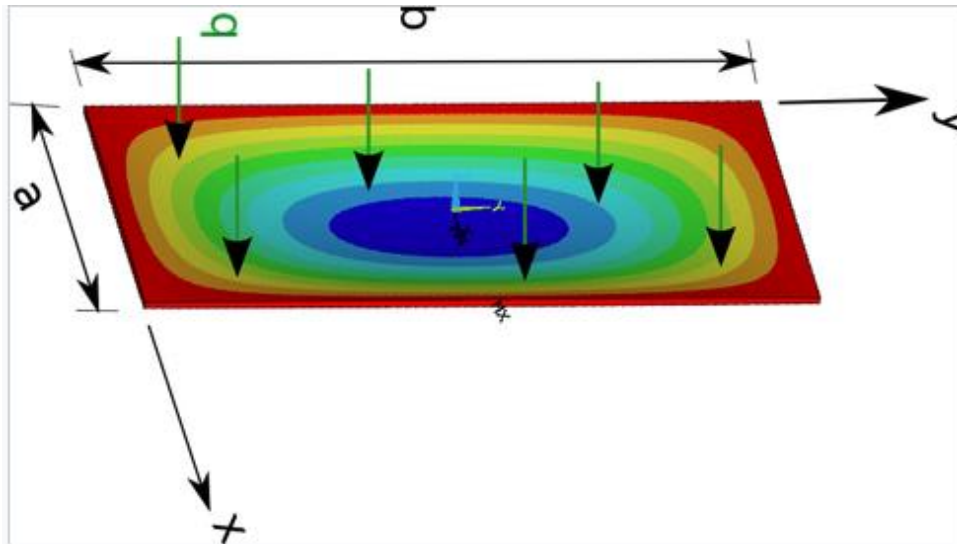


Postoji praktična potreba za analizom sigurnosti po pitanju nestabilnosti izazvanih **kombinacijom geometrije konstrukcije i unutarnjih sila**. U tu svrhu razvila se nova disciplina – **stabilnost konstrukcija**.

# Stabilnost konstrukcija

## Teorija

Problem geometrijske nestabilnosti izražen je pomoću unificiranih **diferencijalnih jednažbi** koje su rezultat kombinacije **kinematičkih** i **materijalnih** izraza, te jednažbi **ravnoteže**.



[18]

$$\frac{\partial^4 w}{\partial x^4} + 2 \frac{\partial^4 w}{\partial x^2 \partial y^2} + \frac{\partial^4 w}{\partial y^4} + \left( \frac{n_x}{D} \frac{\partial^2 w}{\partial x^2} + 2 \frac{\tau_x}{D} \frac{\partial^2 w}{\partial x \cdot \partial y} + \frac{n_y}{D} \frac{\partial^2 w}{\partial y^2} \right) = \frac{q}{D}$$

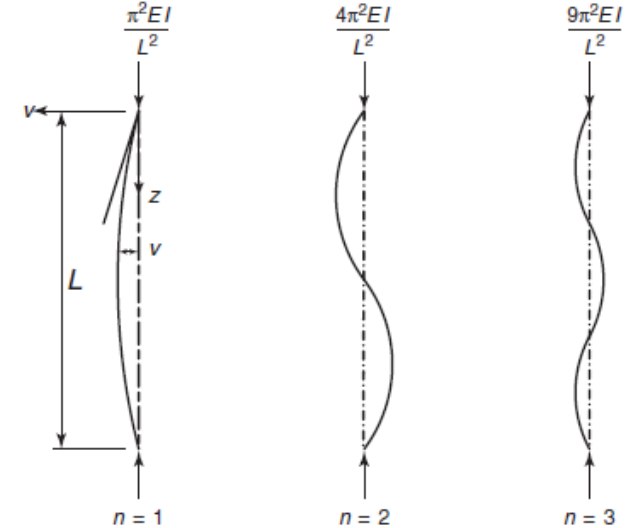


Fig. 2.5 Mode shapes of buckled column.

[19]

$$\frac{d^4 w}{dx^4} + \frac{P}{EI} \frac{d^2 w}{dx^2} = \frac{q}{EI}$$

**Leonhard Euler**  
(1707 – 1783)  
mathematician

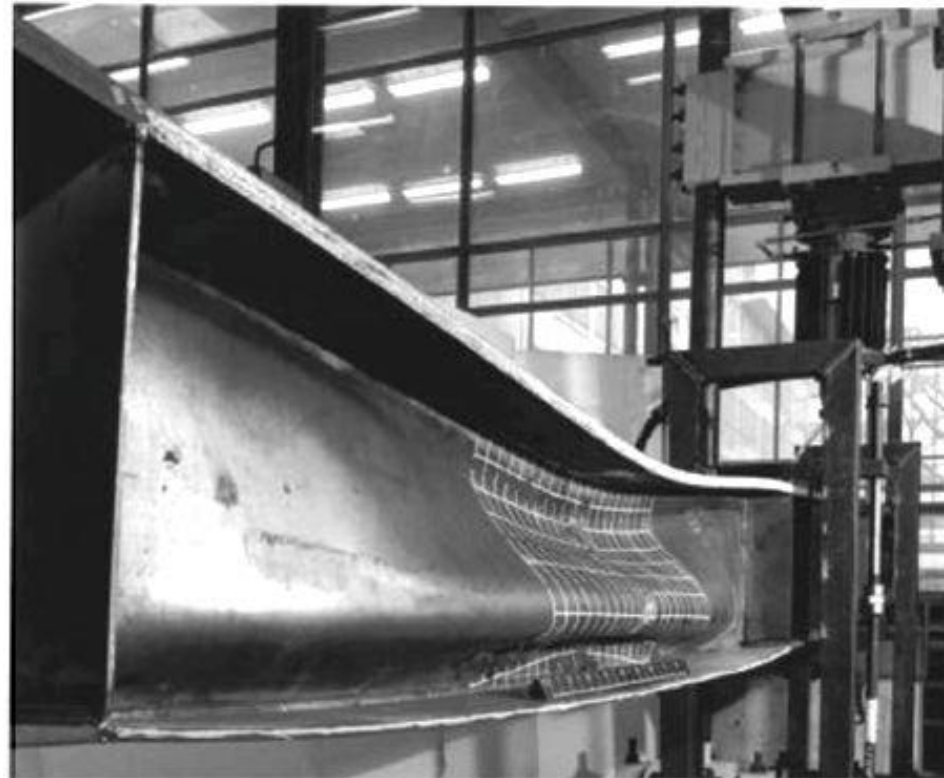


[20]

# Stabilnost konstrukcija

## Eksperimenti

Eksperimentalna postavka modelira praktični problem i potvrđuje teorijske rezultate.



[14]

Figure 2. Vertical web buckling.

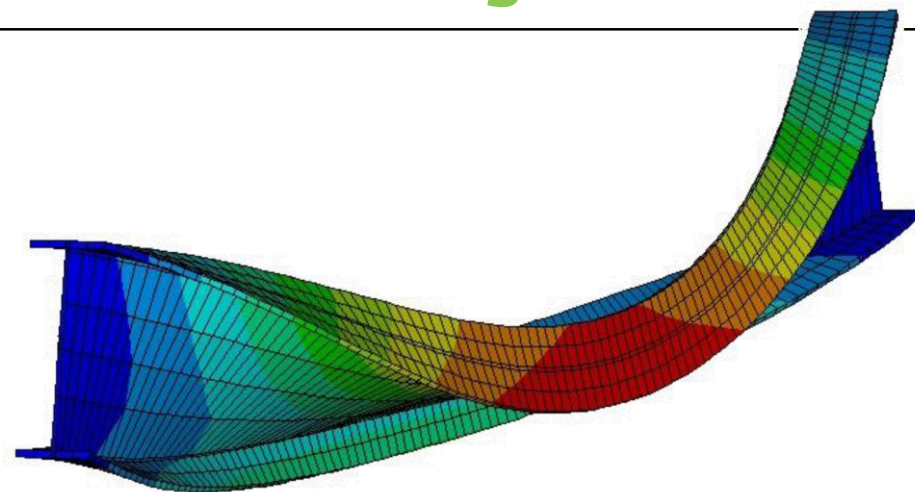
[21]

# Stabilnost konstrukcija

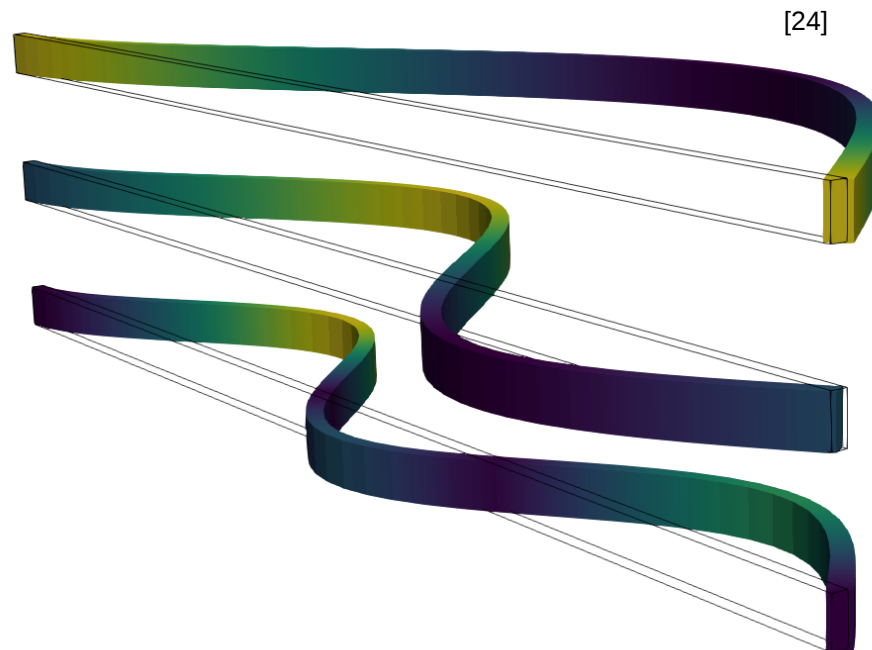
## Numerička rješenja

Numeričkim metodama mogu se riješiti kompleksni praktični problemi.

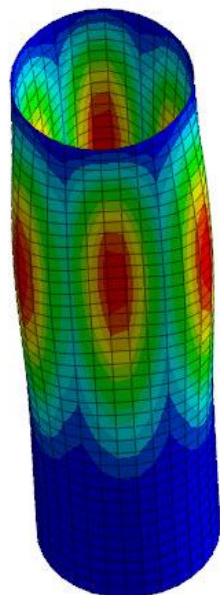
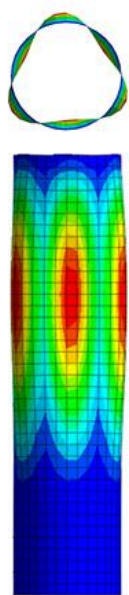
Najčešće korištena je Metoda konačnih elemenata.



[23]



[24]



[22]

# Plošni nosači

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G-329



# Plošni nosači

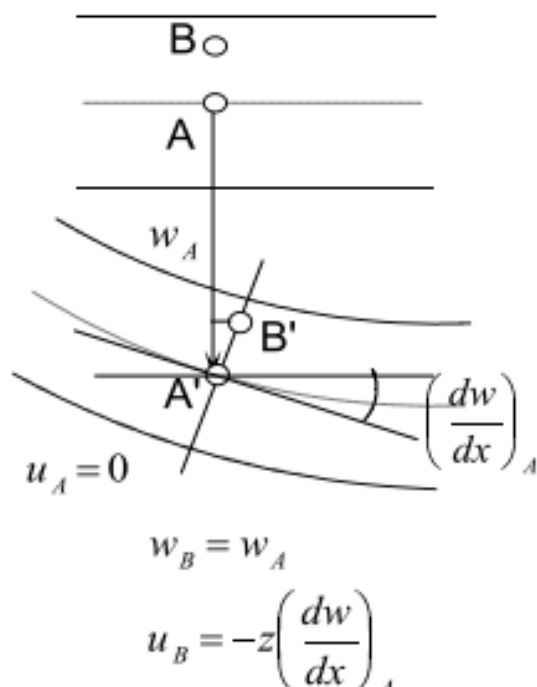


Različiti tipovi plošnih nosača u građevinarstvu: **stijene**, **membrane**, **ploče** i **ljuske**.

# Plošni nosači

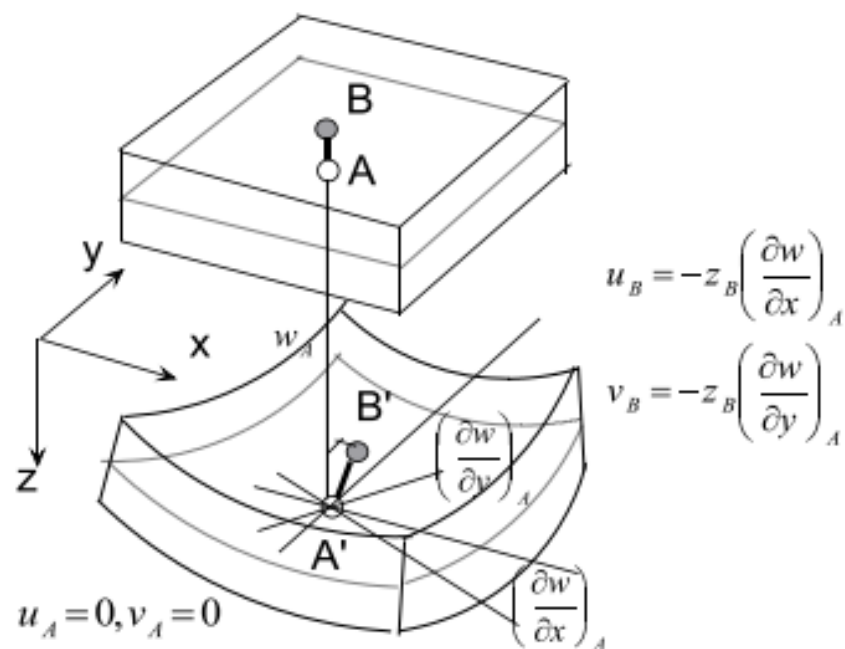
Koja je razlika između **grednih** i **plošnih** nosača?

## Gredni nosač



Pomaci svih točaka određeni su pomacima neutralne osi

## Ploča



Pomaci svih točaka određeni su pomacima neutralne **ravnine**

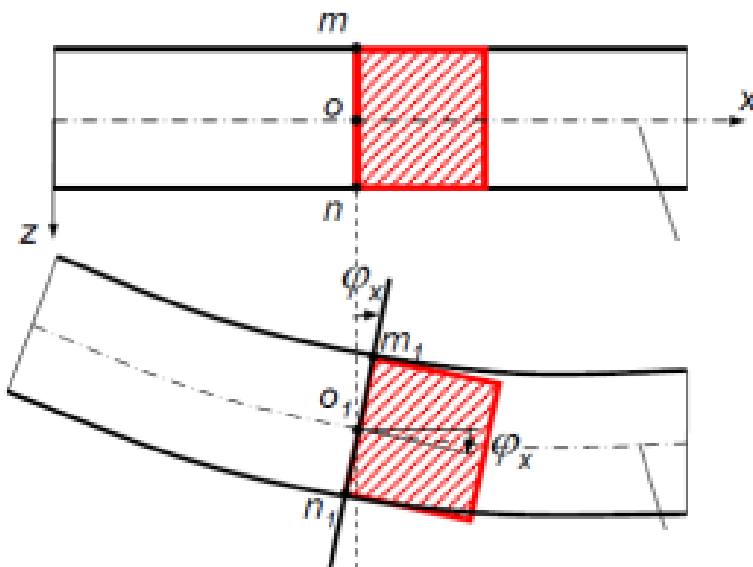
# Plošni nosači

Po čemu se razlikuju **tanke** i **debele (visoke)** ploče?

**Bernouli I + II: Kirchhoff**

$$\varphi_x = \frac{\partial W}{\partial x} \quad \varphi_y = \frac{\partial W}{\partial y}$$

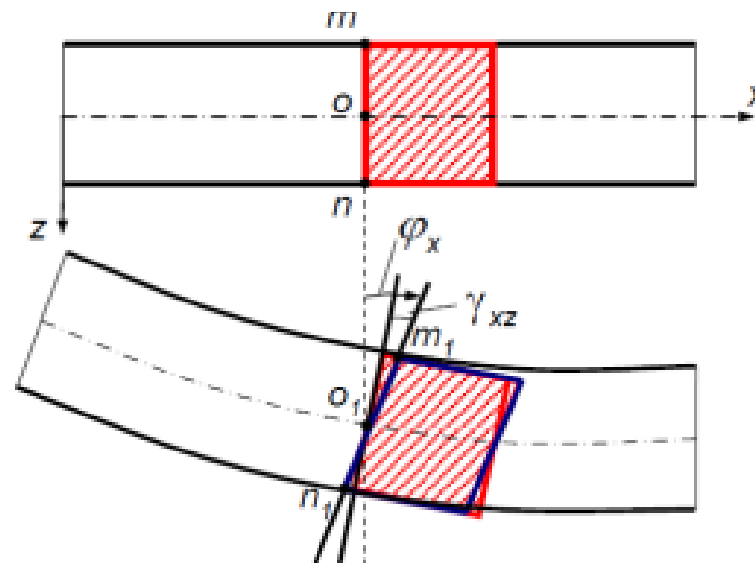
Posmična deformacija se  
zanemaruje



**Bernouli I: Reissner-Mindlin**

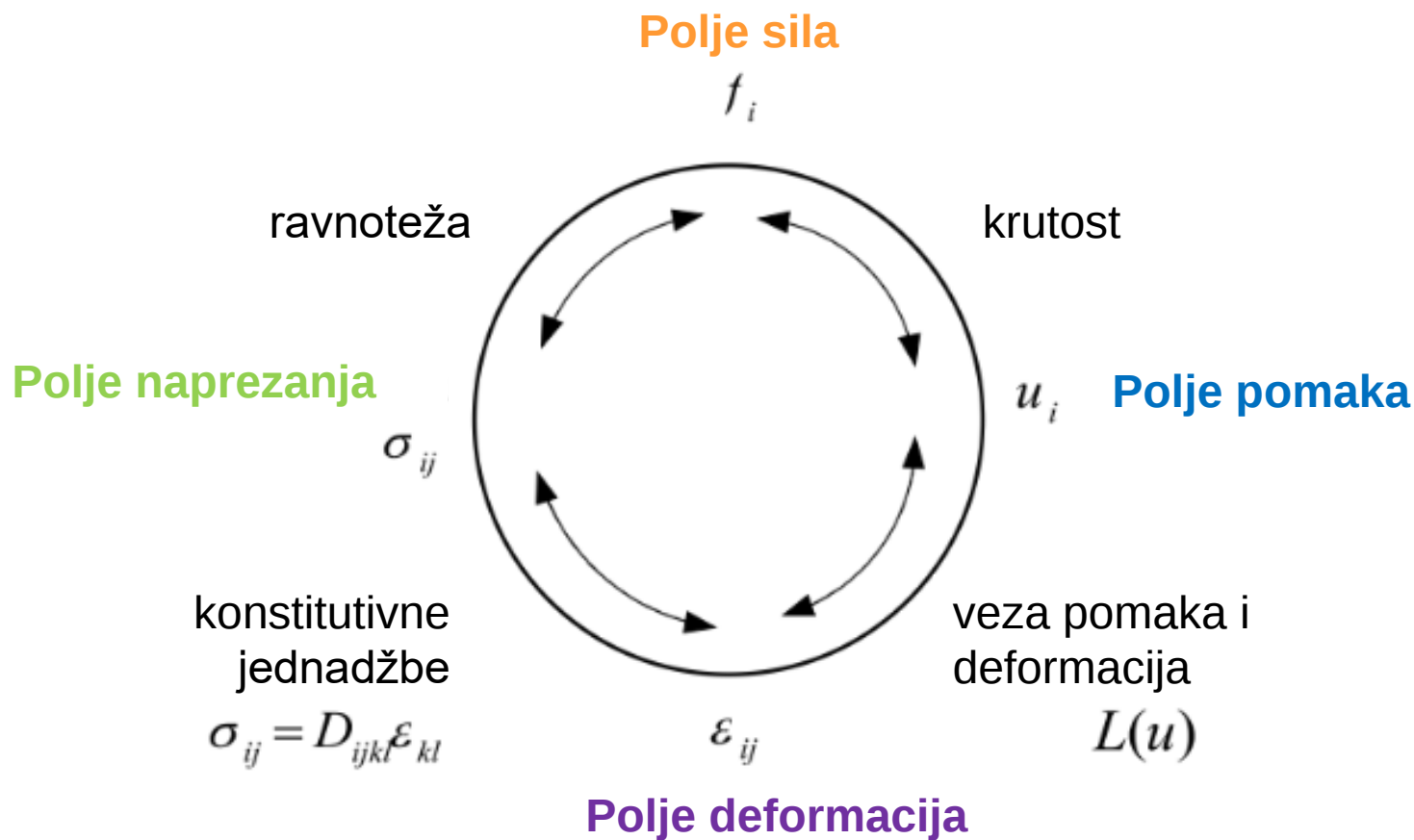
$$\varphi_x = \frac{\partial W}{\partial x} + \gamma_{xz} \quad \varphi_y = \frac{\partial W}{\partial y} + \gamma_{yz}$$

Posmična deformacija se  
**NE** zanemaruje



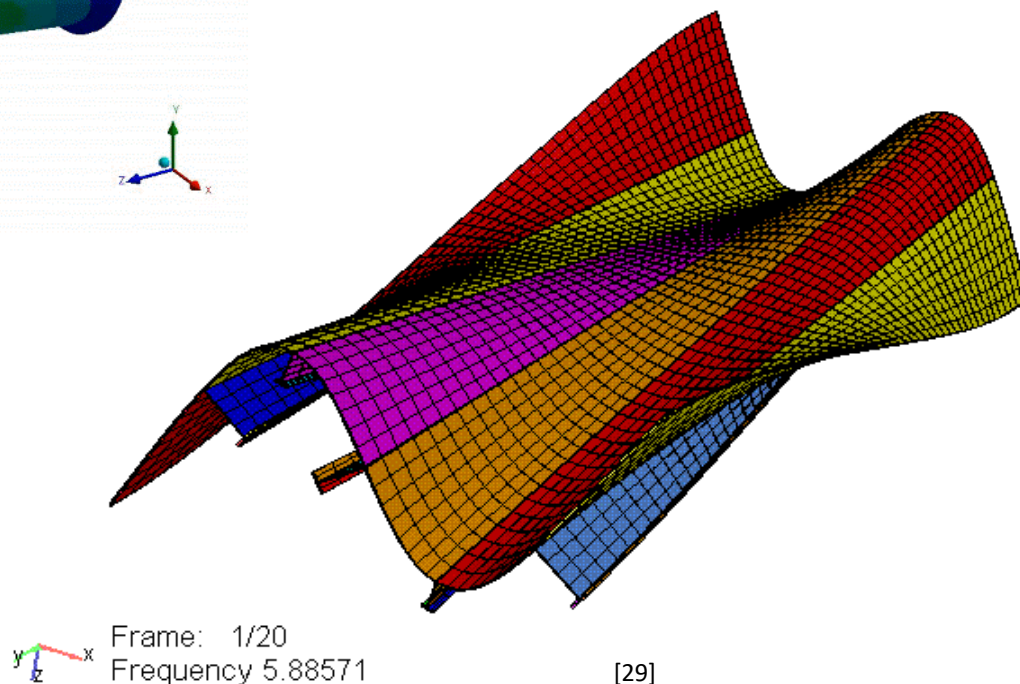
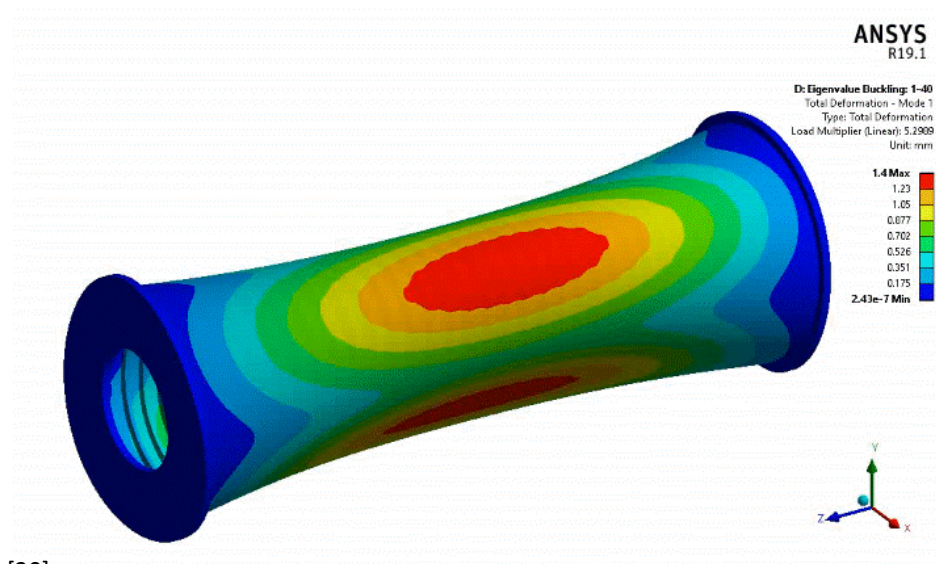
# Plošni nosači

Kako su povezani **sila**, **pomak**, **deformacije** i **naprezanja**?



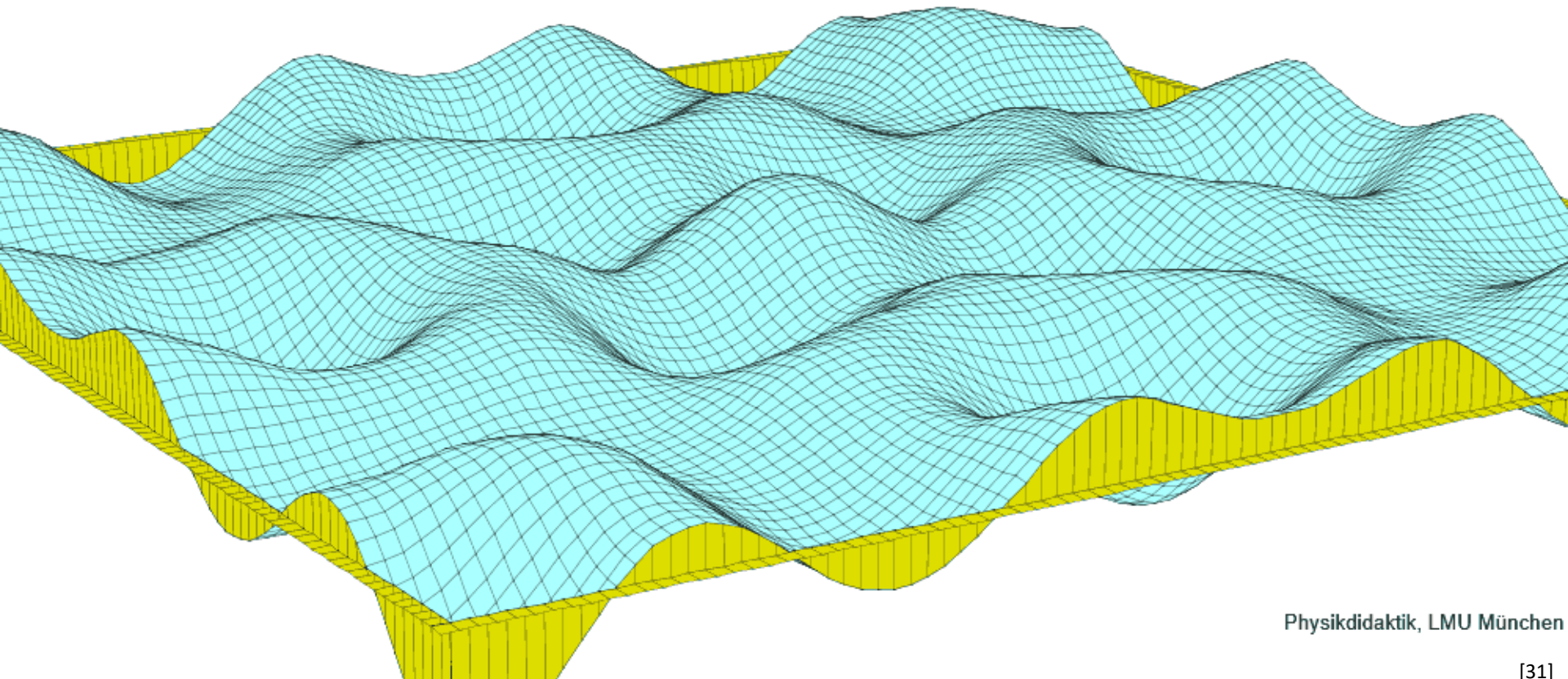
# Plošni nosači

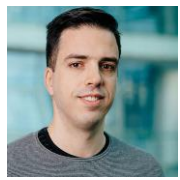
Upoznavanje sa numeričkim procedurama za statičku i dinamičku analizu plošnih nosača – **metoda konačnih razlika, Rayleigh-Ritz metoda te metoda konačnih elemenata.**



# Plošni nosači

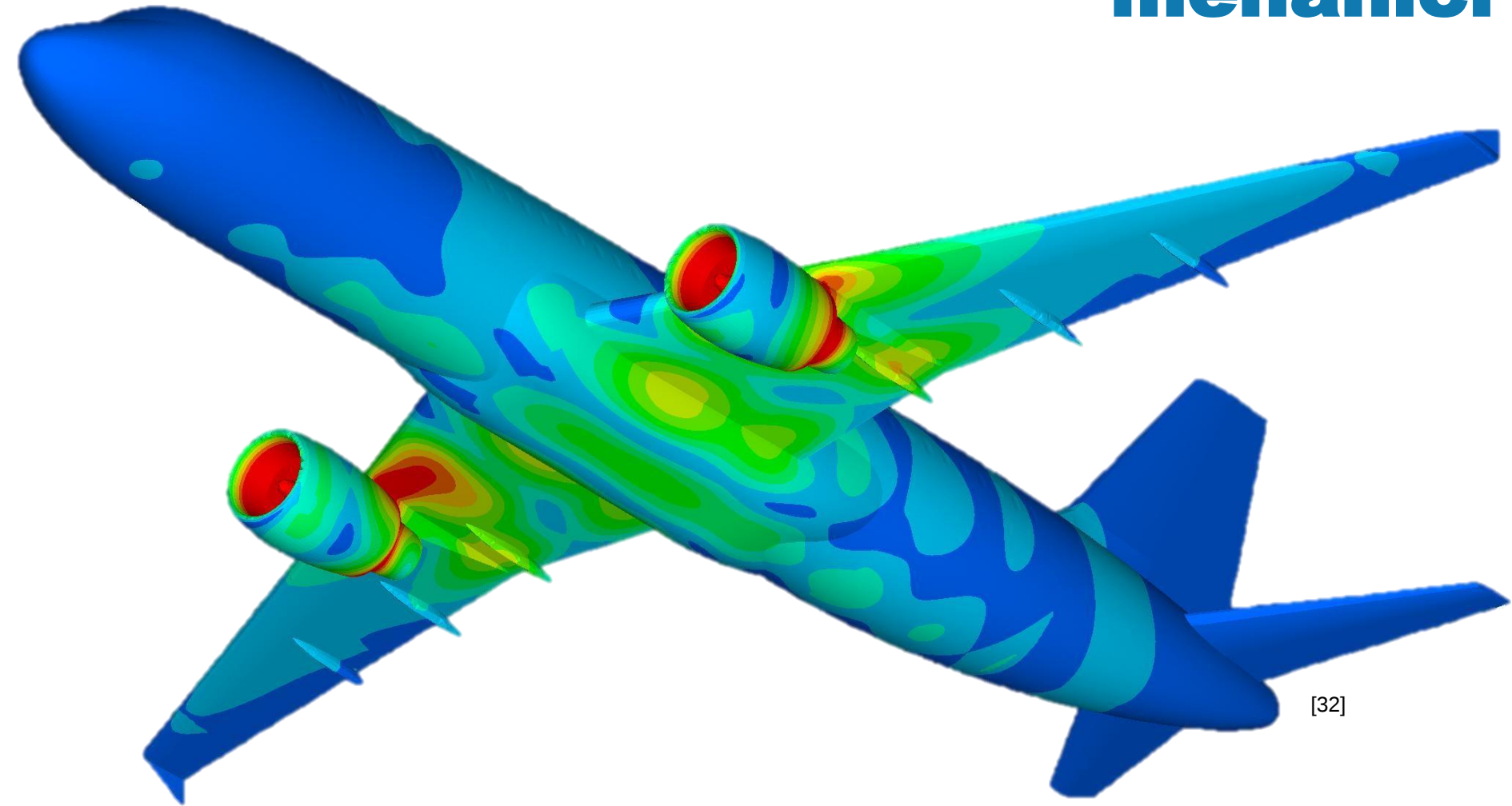
Upoznavanje sa numeričkim procedurama za statičku i dinamičku analizu plošnih nosača – **metoda konačnih razlika**, **Rayleigh-Ritz metoda** te **metoda konačnih elemenata**.





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# Energetske metode u primijenjenoj mehanici



[32]

# Energetske metode u primijenjenoj mehanici

Jaka forma jednačbe kojom opisujemo problem

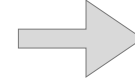
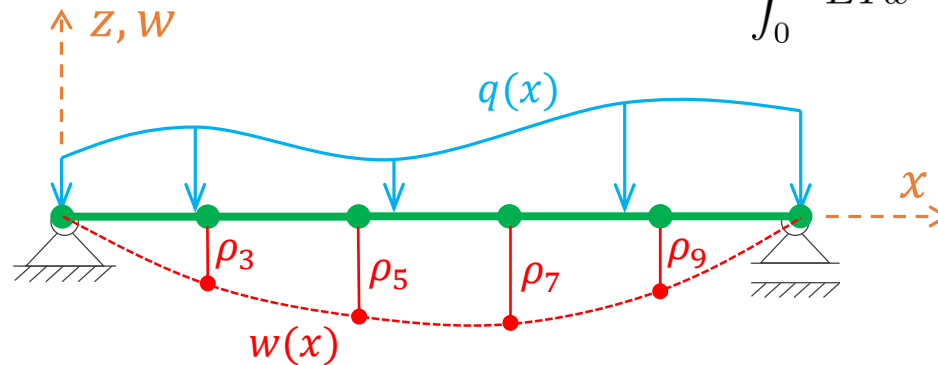
$$EIw^{IV} = q$$

$$w(0) = 0$$

$$w(L) = 0$$

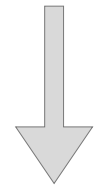
$$w''(0) = 0$$

$$w''(L) = 0$$

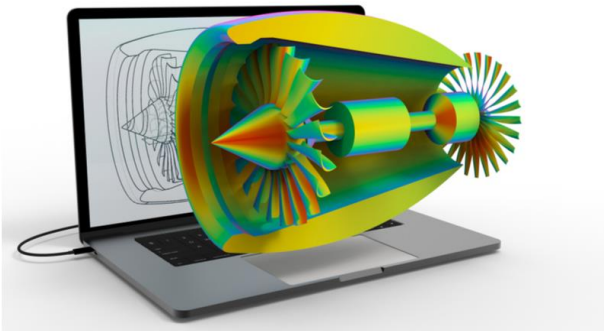


Slaba forma jednačbe kojom opisujemo problem

$$\int_0^L EIw''\bar{w}'' dx - \int_0^L q\bar{w} dx = 0$$



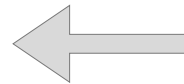
Praktična za implementaciju u računala  
(Metoda konačnih elemenata)



[33]

Približno rješenje jednačbe problema metodom konačnih elemenata

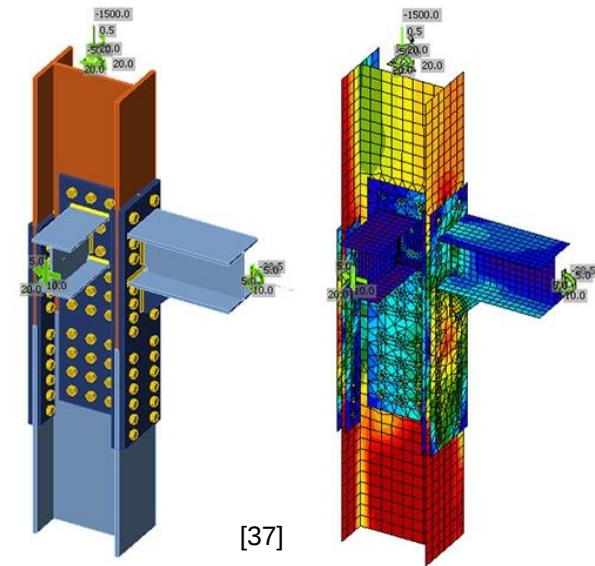
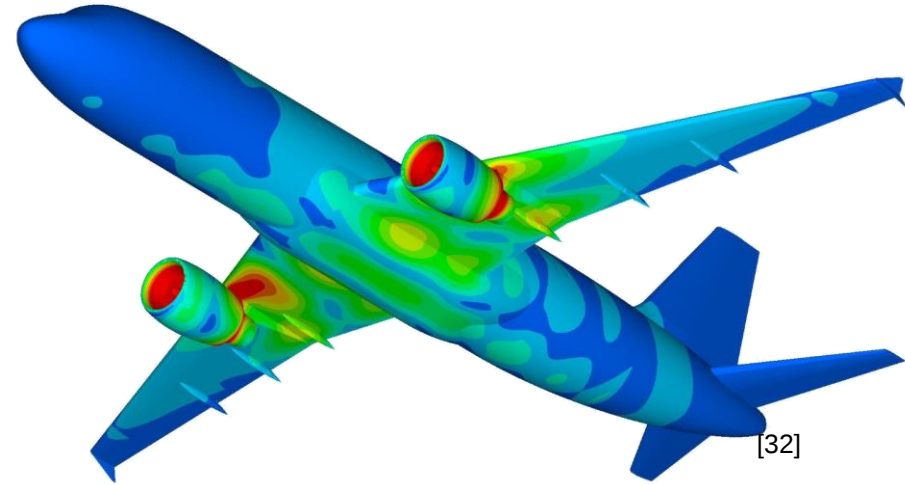
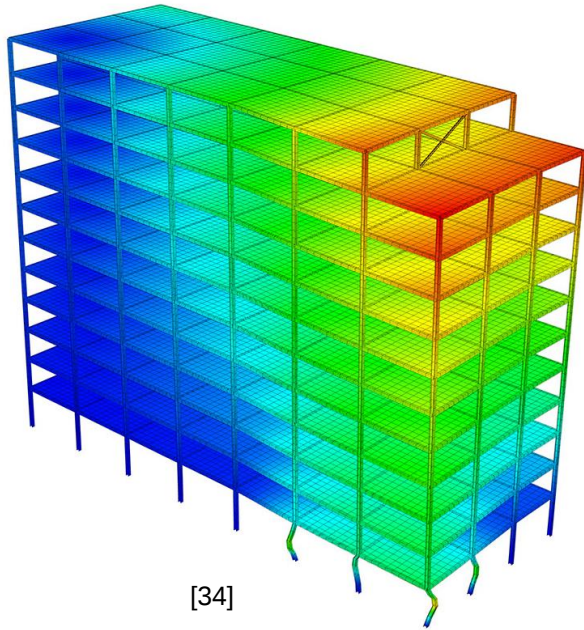
$$\begin{bmatrix} k_{11} & k_{12} & \cdots & k_{1n} \\ k_{21} & k_{22} & \cdots & k_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ k_{n1} & k_{n2} & \cdots & k_{nn} \end{bmatrix} \begin{bmatrix} \rho_1 \\ \rho_2 \\ \vdots \\ \rho_n \end{bmatrix} = \begin{bmatrix} F_1 \\ F_2 \\ \vdots \\ F_n \end{bmatrix}$$



$$\mathbf{K}\boldsymbol{\rho} = \mathbf{F} \rightarrow \boldsymbol{\rho} = \mathbf{K}^{-1}\mathbf{F}$$

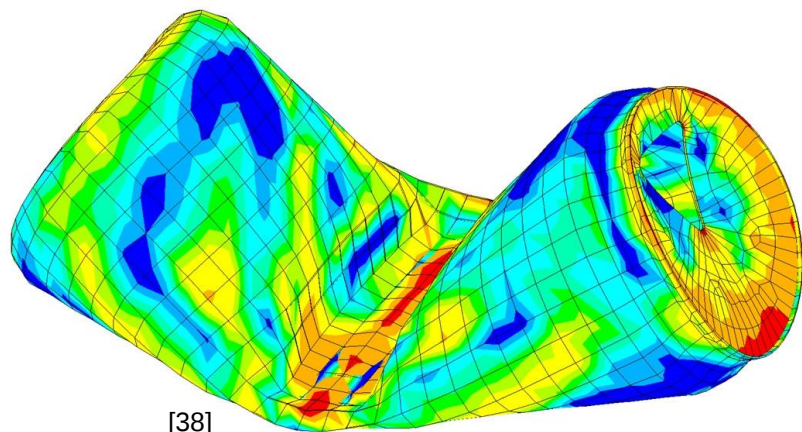
Biti će opisani postupci za dobivanje približnih rješenja koja zadovoljavaju slabu formu, posebice postupak metode konačnih elemenata

# Energetske metode u primijenjenoj mehanici



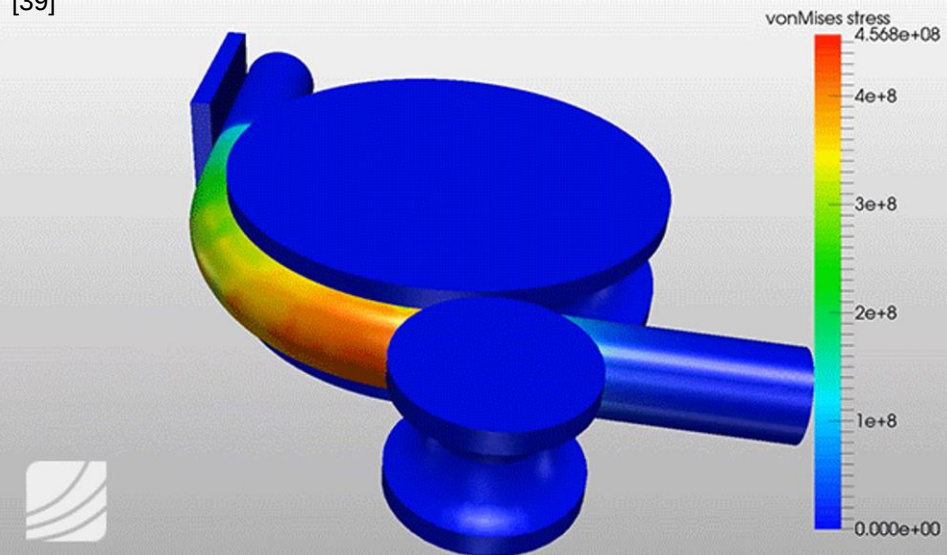
**Pomoću softvera koji implementira Metodu konačnih elemenata moguće je analizirati širok spektar kompleksnih mehaničkih problema**

# Energetske metode u primijenjenoj mehanici

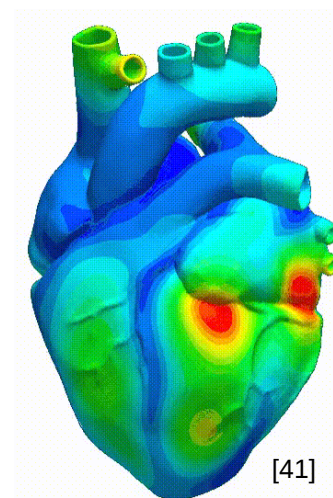
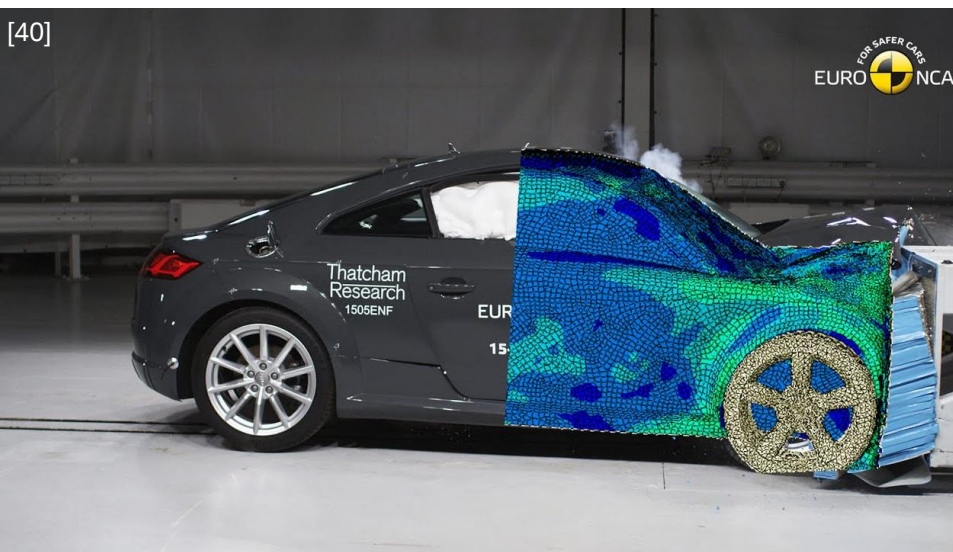


[38]

[39]



[40]



[41]

**Pomoću softvera koji implementira Metodu konačnih elemenata moguće je analizirati širok spektar kompleksnih mehaničkih problema**



prof. **Leo Škec**  
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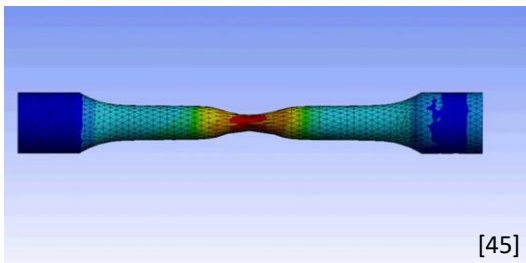
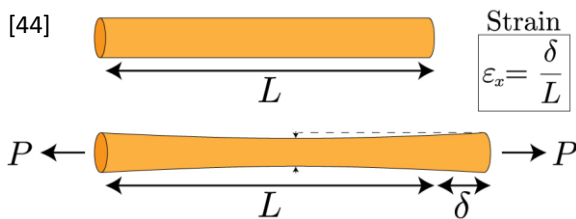
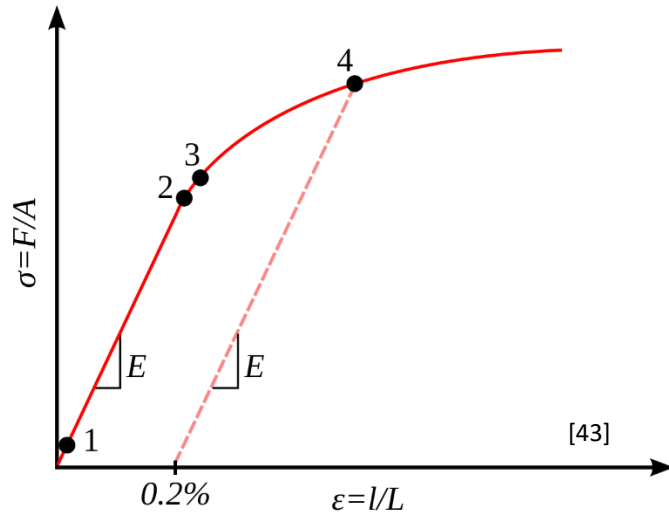


# Uvod u modeliranje plastičnosti i oštećenja

# Uvod u modeliranje plastičnosti i oštećenja

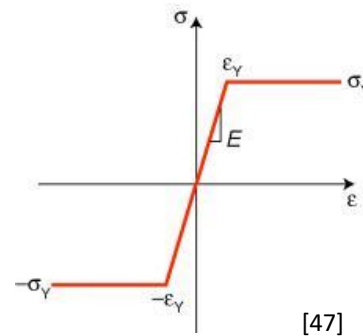
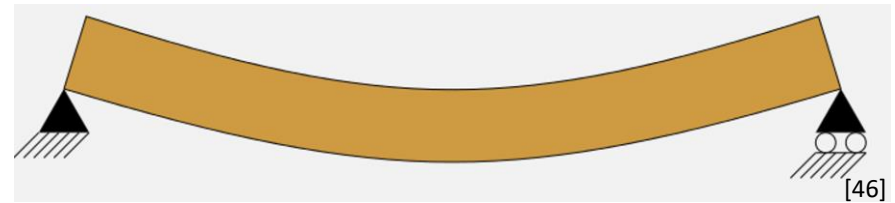
## JEDNOOSNO STANJE NAPREZANJA

- Plastične deformacije

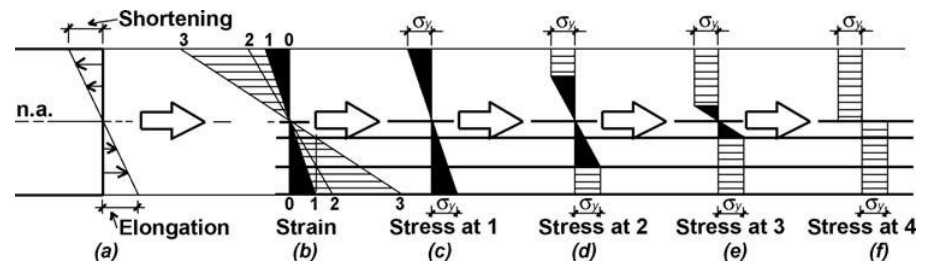
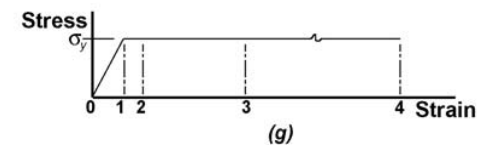


## ELASTO-PLASTIČNO SAVIJANJE

- postepena plastifikacija poprečnog presjeka i otvaranje plastičnog zgloba

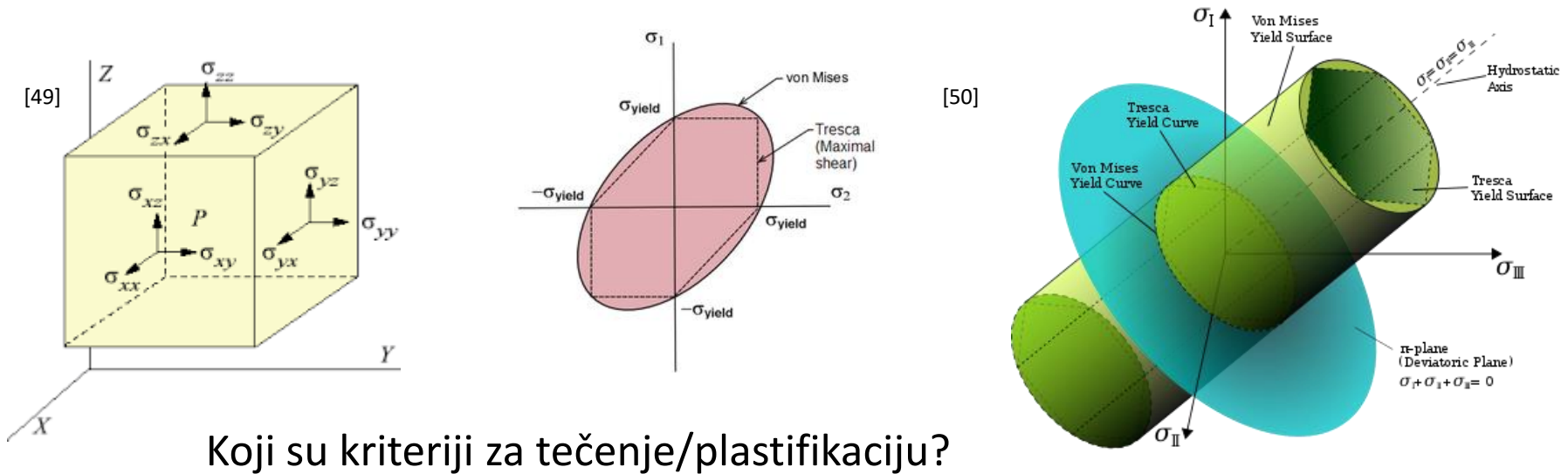


## Prandtlov model

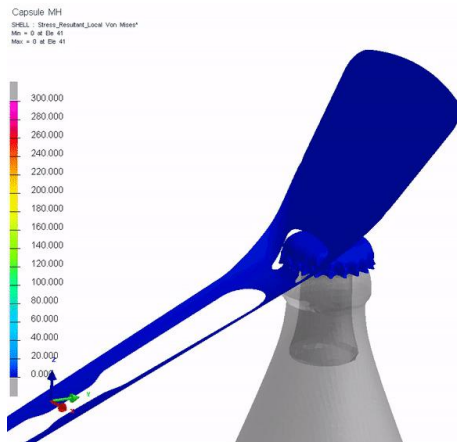


# Uvod u modeliranje plastičnosti i oštećenja

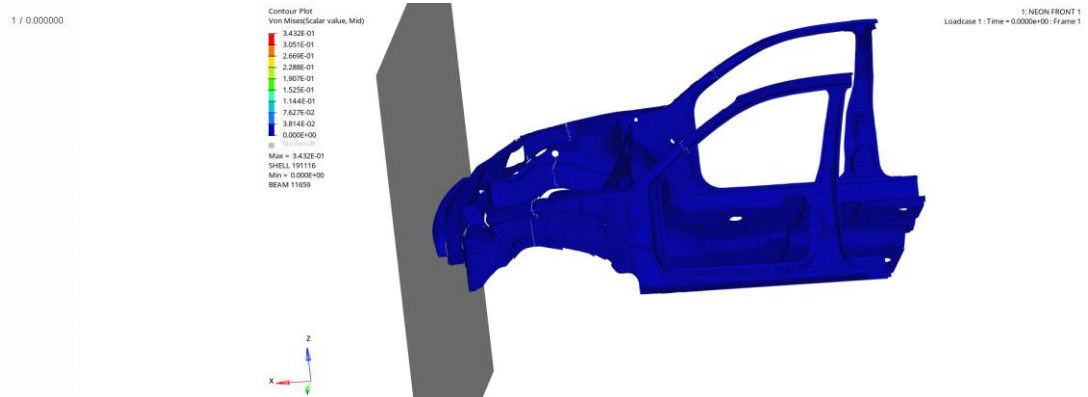
## VIŠEOSNO STANJE NAPREZANJA – kada nastupa tečenje/plastifikacija?



## Primjena u računalnim simulacijama



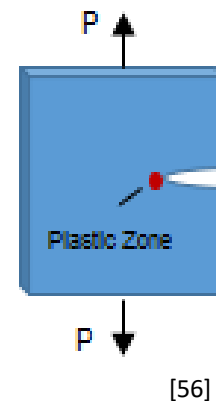
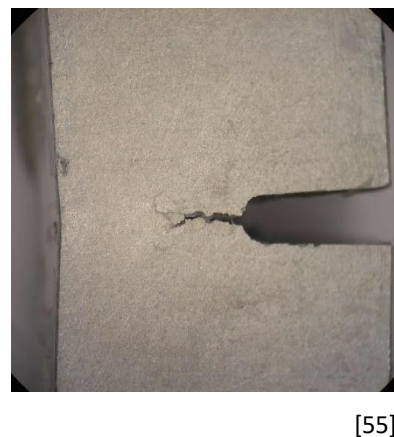
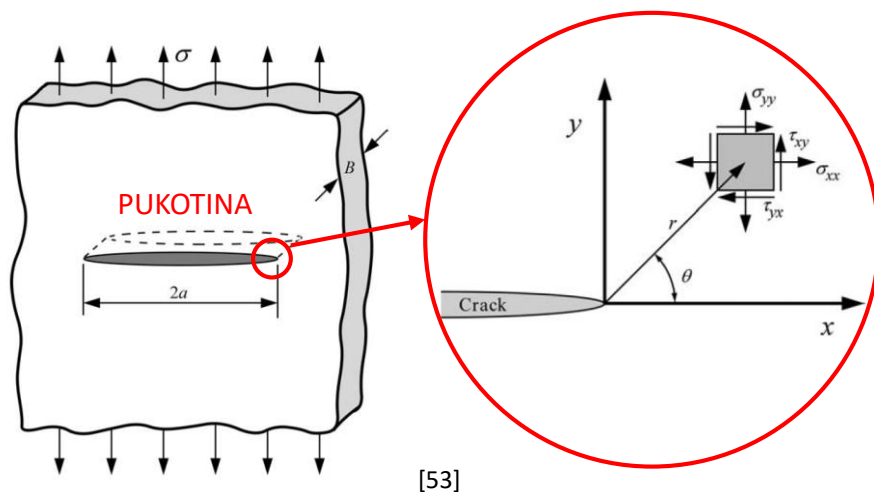
[51]



[52]

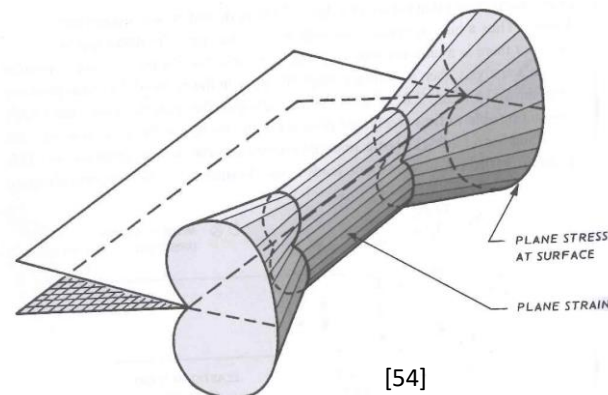
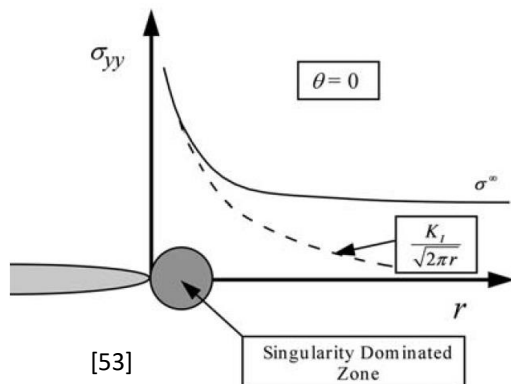
# Uvod u modeliranje plastičnosti i oštećenja

**MEHANIKA LOMA** – kada i zašto nastaje pukotina u materijalu?



**Linearno-elastična mehanika loma** – kruti slom materijala

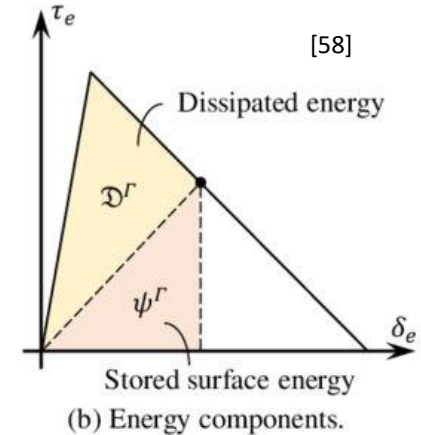
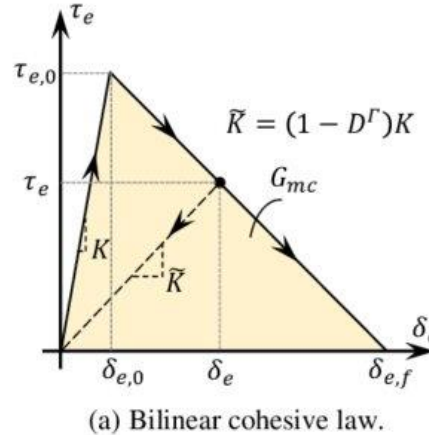
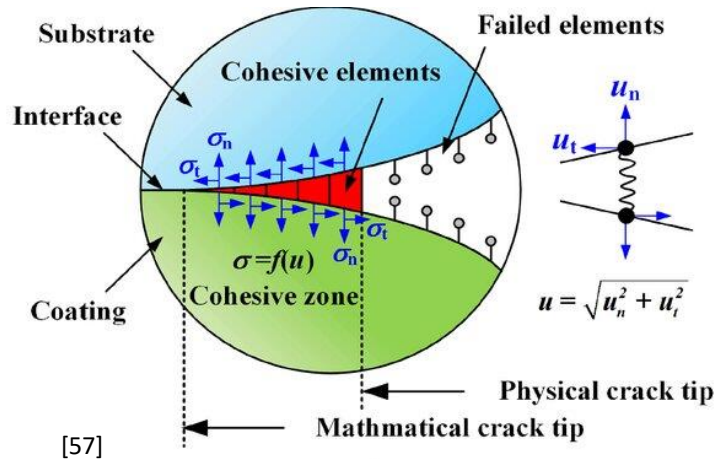
**Duktilni slom materijala** - iza pukotine formira se plastična zona (oštećenje)



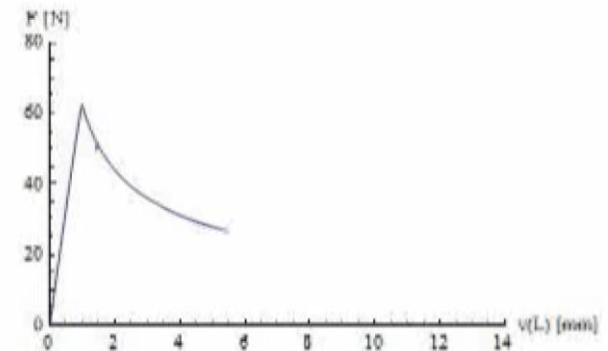
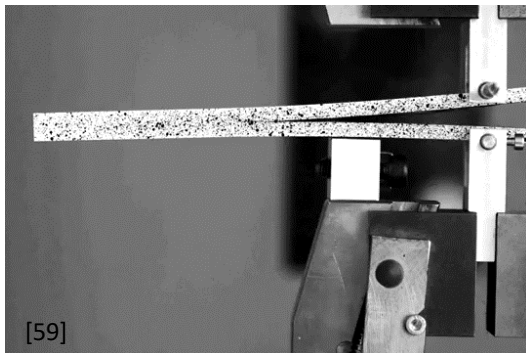
# Uvod u modeliranje plastičnosti i oštećenja

## MEHANIKA OŠTEĆENJA

- Modeli progresivnog oštećenja (omekšanja) koji dovode do sloma materijala



Eksperimentalno određivanje parametara koji opisuju lomnu otpornost materijala



# PRIMIJENJENA

# MEHANIKA U SUVREMENOJ

# INŽENJERSKOJ PRAKSI

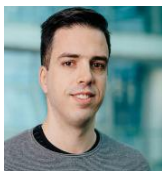
Detaljan opis predmeta na [www.gradri.hr](http://www.gradri.hr):

<https://gradri.uniri.hr/wp-content/uploads/2023/07/Diplomski-sveucilisni-2023-svibanj.pdf>

Za dodatne informacije:



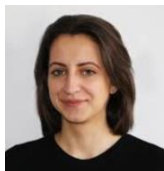
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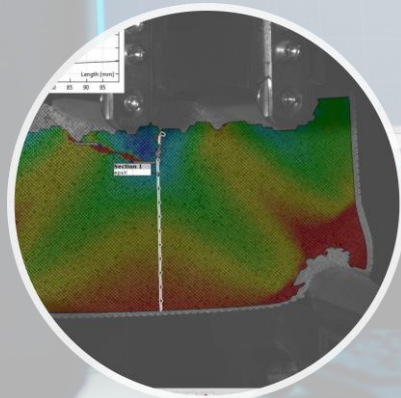
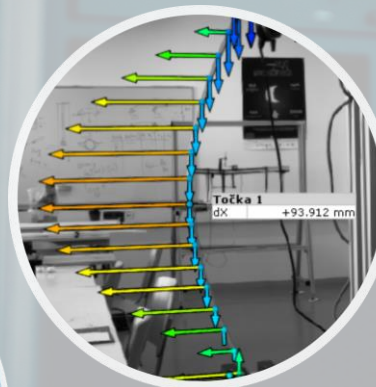
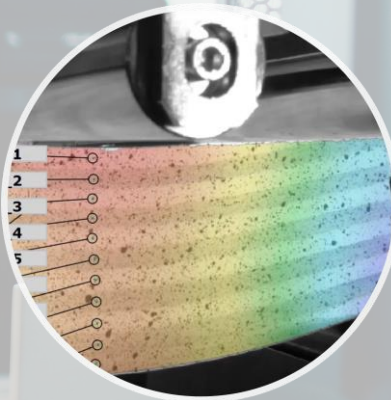
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**NAPOMENA:** *Moguće je upisati samo dio predmeta mikrokvalifikacije, ali se onda ne stječe mikrokvalifikacija.*

# PRIMIJENJENA MEHANIKA U SUVREMENOJ INŽENJERSKOJ PRAKSI



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